



# Assignment

## Measurement of Angles, Trigonometrical Ratios, Function and

### Basic Level

- Which of the following relation is correct [WB JEE 1991]  
(a)  $\sin 1^\circ > \sin 1$  (b)  $\sin 1 > \sin 1^\circ$  (c)  $\sin 1 = \sin 1^\circ$  (d)  $\frac{\pi}{180} \sin 1 = \sin 1^\circ$
- The radius of the circle whose arc of length 15 cm makes an angle of  $3/4$  radian at the centre is  
(a) 10 cm (b) 20 cm (c)  $11\frac{1}{4}$  cm (d)  $22\frac{1}{2}$  cm
- If  $\tan \theta = \frac{-4}{3}$ , then  $\sin \theta =$  [Orissa JEE 2002; IIT 1979]  
(a)  $\frac{-4}{5}$  but not  $\frac{4}{5}$  (b)  $-\frac{4}{5}$  or  $\frac{4}{5}$  (c)  $\frac{4}{5}$  but not  $-\frac{4}{5}$  (d) None of these
- If  $f(x) = \cos^2 x + \sec^2 x$ , then  
(a)  $f(x) < 1$  (b)  $f(x) = 1$  (c)  $1 < f(x) < 2$  (d)  $f(x) \geq 2$
- If  $x = \sec \theta + \tan \theta$ , then  $x + \frac{1}{x} =$   
(a) 1 (b)  $2 \sec \theta$  (c) 2 (d)  $2 \tan \theta$
- If A lies in the second quadrant and  $3 \tan A + 4 = 0$  then the value of  $2 \cot A - 5 \cos A + \sin A$  is equal to [Harayana CEE 1999]  
(a)  $\frac{-53}{10}$  (b)  $\frac{-7}{10}$  (c)  $\frac{7}{10}$  (d)  $\frac{23}{10}$
- $\tan 1^\circ \tan 2^\circ \tan 3^\circ \tan 4^\circ \dots \dots \dots \tan 89^\circ =$  [MP PET 1998, 2001]  
(a) 1 (b) 0 (c)  $\infty$  (d)  $1/2$
- The incorrect statement is  
(a)  $\sin \theta = -\frac{1}{5}$  (b)  $\cos \theta = 1$  (c)  $\sec \theta = \frac{1}{2}$  (d)  $\tan \theta = 20$
- If  $\cos \theta - \sin \theta = \sqrt{2} \sin \theta$ , then  $\cos \theta + \sin \theta$  is equal to [WB JEE 1988]  
(a)  $\sqrt{2} \cos \theta$  (b)  $\sqrt{2} \sin \theta$  (c)  $2 \cos \theta$  (d)  $-\sqrt{2} \cos \theta$
- If  $\sec \theta + \tan \theta = p$ , then  $\tan \theta$  is equal to [MP PET 1994]  
(a)  $\frac{2p}{p^2 - 1}$  (b)  $\frac{p^2 - 1}{2p}$  (c)  $\frac{p^2 + 1}{2p}$  (d)  $\frac{2p}{p^2 + 1}$
- If  $\sin \theta - \cos \theta = 1$ , then  $\sin \theta \cos \theta =$  [Karnataka CET 1998]  
(a) 0 (b) 1 (c) 2 (d)  $1/2$
- The value of  $\cos 1^\circ \cos 2^\circ \cos 3^\circ \dots \dots \cos 179^\circ$  is [Karnataka CET 1999]



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- (a)  $\frac{1}{\sqrt{2}}$  (b) 0 (c) 1 (d) None of these
13. If  $\tan \theta = +\frac{1}{\sqrt{5}}$  and  $\theta$  lies in the 1<sup>st</sup> quadrant, then  $\cos \theta$  is  
 (a)  $\frac{1}{\sqrt{6}}$  (b)  $-\frac{1}{\sqrt{6}}$  (c)  $\frac{\sqrt{5}}{\sqrt{6}}$  (d)  $-\frac{\sqrt{5}}{\sqrt{6}}$
14. If A lies in the third quadrant and  $3 \tan A - 4 = 0$ , then  $5 \sin 2A + 3 \sin A + 4 \cos A =$  [EAMCET 1994]  
 (a) 0 (b)  $-\frac{24}{5}$  (c)  $\frac{24}{5}$  (d)  $\frac{48}{5}$
15.  $(\sec^2 \theta - 1)(\operatorname{cosec}^2 \theta - 1) =$  [Karnataka CET 1998]  
 (a) 0 (b) 1 (c)  $\sec \theta \cdot \operatorname{cosec} \theta$  (d)  $\sin^2 \theta - \cos^2 \theta$
16. If  $\tan \theta = \frac{20}{21}$ ,  $\cos \theta$  will be [MP PET 1994]  
 (a)  $\pm \frac{20}{41}$  (b)  $\pm \frac{1}{21}$  (c)  $\pm \frac{21}{29}$  (d)  $\pm \frac{20}{21}$
17. If  $\operatorname{cosec} A + \cot A = \frac{11}{2}$ , then  $\tan A$  equal to [Roorkee 1995]  
 (a)  $\frac{21}{22}$  (b)  $\frac{15}{16}$  (c)  $\frac{44}{117}$  (d)  $\frac{117}{43}$
18. If  $\sin \theta = \frac{24}{25}$  and  $\theta$  lies in the second quadrant, then  $\sec \theta + \tan \theta$  equal to [MP PET 1997]  
 (a) -3 (b) -5 (c) -7 (d) -9
19. If  $5 \tan \theta = 4$ , then  $\frac{5 \sin \theta - 3 \cos \theta}{5 \sin \theta + 2 \cos \theta}$  equal to [Karnataka CET 1998]  
 (a) 0 (b) 1 (c)  $1/6$  (d) 6
20.  $\frac{1 + \cos \theta}{\sin^2 \theta}$  equal to [Karnataka CET 1998]  
 (a) 0 (b) 1 (c)  $\frac{1}{1 - \cos \theta}$  (d)  $\frac{1}{1 + \cos \theta}$
21. The expression  $\frac{1}{\tan A + \cot A}$  simplifies to [SCRA 1999]  
 (a)  $\sec A \operatorname{cosec} A$  (b)  $\sin A \cos A$  (c)  $\tan 2A$  (d)  $\sin 2A$
22. If for real values of  $x$ ,  $\cos \theta = x + \frac{1}{x}$ , then [MP PET 1996]  
 (a)  $\theta$  is an acute angle (b)  $\theta$  is a right angle (c)  $\theta$  is an obtuse angle (d) No value of  $\theta$  is possible
23. If  $\sin x + \operatorname{cosec} x = 2$ , then  $\sin^n x + \operatorname{cosec}^n x$  is equal to [UPSEAT 2002]  
 (a) 2 (b)  $2^n$  (c)  $2^{n-1}$  (d)  $2^{n-2}$

### Advance Level

24. One root of the equation  $\cos x - x + \frac{1}{2} = 0$  lies in the interval  
 (a)  $\left[0, \frac{\pi}{2}\right]$  (b)  $\left[-\frac{\pi}{2}, 0\right]$  (c)  $\left[\frac{\pi}{2}, \pi\right]$  (d)  $\left[\pi, \frac{3\pi}{2}\right]$

25. If  $\frac{2 \sin \alpha}{\{1 + \cos \alpha + \sin \alpha\}} = y$ , then  $\frac{\{1 - \cos \alpha + \sin \alpha\}}{1 + \sin \alpha} =$  [BIT Ranchi 1996]
- (a)  $\frac{1}{y}$  (b)  $y$  (c)  $1 - y$  (d)  $1 + y$
26. If  $\sin \theta + \sin^2 \theta + \sin^3 \theta = 1$ , then  $\cos^6 \theta - 4 \cos^4 \theta + 8 \cos^2 \theta =$
- (a) 4 (b) 2 (c) 1 (d) None of these
27. If  $\theta$  and  $\phi$  are angles in the 1<sup>st</sup> quadrant such that  $\tan \theta = 1/7$  and  $\sin \phi = 1/\sqrt{10}$ . Then
- (a)  $\theta + 2\phi = 90^\circ$  (b)  $\theta + 2\phi = 60^\circ$  (c)  $\theta + 2\phi = 30^\circ$  (d)  $\theta + 2\phi = 45^\circ$
28. The value of  $\theta$  lying between 0 and  $\pi/2$  and satisfying the equation  $\begin{vmatrix} 1 + \sin^2 \theta & \cos^2 \theta & 4 \sin 4\theta \\ \sin^2 \theta & 1 + \cos^2 \theta & 4 \sin 4\theta \\ \sin^2 \theta & \cos^2 \theta & 1 + 4 \sin 4\theta \end{vmatrix} = 0$
- [IIT 1988; MNR 1992; Kurukshetra CEE 1998; DCE 1996]
- (a)  $\frac{7\pi}{24}$  or  $\frac{11\pi}{24}$  (b)  $\frac{5\pi}{24}$  (c)  $\frac{\pi}{24}$  (d) None of these
29. If  $\frac{3\pi}{4} < \alpha < \pi$ , then  $\sqrt{\operatorname{cosec}^2 \alpha + 2 \cot \alpha}$  is equal to [Pb. CET 2000, AMU 2001]
- (a)  $1 + \cot \alpha$  (b)  $1 - \cot \alpha$  (c)  $-1 - \cot \alpha$  (d)  $-1 + \cot \alpha$
30. If for all real values of  $x$ ,  $\frac{4x^2 + 1}{64x^2 - 96x \sin \alpha + 5} < \frac{1}{32}$ , then  $\alpha$  lies in the interval [Roorkee 1998]
- (a)  $\left(0, \frac{\pi}{3}\right)$  (b)  $\left(\frac{\pi}{3}, \frac{2\pi}{3}\right)$  (c)  $\left(\frac{2\pi}{3}, \pi\right)$  (d)  $\left(\frac{4\pi}{3}, \frac{5\pi}{3}\right)$
31. If  $\tan \theta = \sqrt{\frac{3}{2}}$ , then the sum of the infinite series  $1 + 2(1 - \cos \theta) + 3(1 - \cos \theta)^2 + 4(1 - \cos \theta)^3 + \dots \infty$  is
- (a)  $\frac{2}{3}$  (b)  $\frac{\sqrt{3}}{4}$  (c)  $\frac{5}{2\sqrt{2}}$  (d)  $\frac{5}{2}$
32. Let  $A_0A_1A_2A_3A_4A_5$  be a regular hexagon inscribed in a circle of unit radius. Then the product of the lengths of the line segments  $A_0A_1$ ,  $A_0A_2$  and  $A_0A_4$  is
- (a)  $\frac{3}{4}$  (b)  $3\sqrt{3}$  (c) 3 (d)  $\frac{3\sqrt{3}}{2}$

## Trigonometrical Ratios of Allied Angles

## Basic Level

33. If  $x \sin 45^\circ \cos^2 60^\circ = \frac{\tan^2 60^\circ \operatorname{cosec} 30^\circ}{\sec 45^\circ \cot^2 30^\circ}$ , then  $x =$  [Kerala (Engg.) 2002]
- (a) 2 (b) 4 (c) 8 (d) 16
34.  $\cos A + \sin(270^\circ + A) - \sin(270^\circ - A) + \cos(180^\circ + A) =$  [MP PET 1990]
- (a) -1 (b) 0 (c) 1 (d) None of these
35.  $\sin(\pi + \theta) \sin(\pi - \theta) \operatorname{cosec}^2 \theta =$  [EAMCET 1980]
- (a) 1 (b) -1 (c)  $\sin \theta$  (d)  $-\sin \theta$
36. The value of  $\sin 600^\circ \cos 330^\circ + \cos 120^\circ \sin 150^\circ$  is [MP PET 1994]

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- (a) -1 (b) 1 (c)  $\frac{1}{\sqrt{2}}$  (d)  $\frac{\sqrt{3}}{2}$
37. If  $A = 130^\circ$  and  $x = \sin A + \cos A$ , then [Karnataka CET 1989]  
 (a)  $x > 0$  (b)  $x < 0$  (c)  $x = 0$  (d)  $x \leq 0$
38.  $\tan \theta \sin\left(\frac{\pi}{2} + \theta\right) \cos\left(\frac{\pi}{2} - \theta\right) =$  [EAMCET 1981]  
 (a) 1 (b) 0 (c)  $\frac{1}{\sqrt{2}}$  (d) None of these
39.  $\sin^2 5^\circ + \sin^2 10^\circ + \sin^2 15^\circ + \dots + \sin^2 85^\circ + \sin^2 90^\circ =$  [Karnataka CET 1999, 1995]  
 (a) 7 (b) 8 (c) 9 (d)  $9\frac{1}{2}$
40. Values of  $\theta (0 < \theta < 360^\circ)$  satisfying  $\operatorname{cosec} \theta + 2 = 0$  are [EAMCET 1994]  
 (a)  $210^\circ, 300^\circ$  (b)  $240^\circ, 300^\circ$  (c)  $210^\circ, 240^\circ$  (d)  $210^\circ, 330^\circ$
41. The value of  $\tan(-945^\circ)$  is [MP PET 1997]  
 (a) -1 (b) -2 (c) -3 (d) -4
42. The value of  $\frac{\cot 54^\circ}{\tan 36^\circ} + \frac{\tan 20^\circ}{\cot 70^\circ}$  is [Karnataka CET 1999]  
 (a) 2 (b) 3 (c) 1 (d) 0
43.  $\tan 9^\circ - \tan 27^\circ - \tan 63^\circ + \tan 81^\circ =$  [Roorkee 1989]  
 (a)  $1/2$  (b) 2 (c) 4 (d) 8
44.  $\cos 1^\circ + \cos 2^\circ + \cos 3^\circ + \dots + \cos 180^\circ =$  [Karnataka CET 2003]  
 (a) 0 (b) 1 (c) -1 (d) 2
45. If  $\tan(A - B) = 1$ ,  $\sec(A + B) = \frac{2}{\sqrt{3}}$ , then the smallest positive value of  $B$  is [Kerala (Engg.) 2002]  
 (a)  $\frac{25}{24}\pi$  (b)  $\frac{19}{24}\pi$  (c)  $\frac{13}{24}\pi$  (d)  $\frac{11}{24}\pi$
46. If  $x = \sin 130^\circ \cos 80^\circ$ ,  $y = \sin 80^\circ \cos 130^\circ$ ,  $z = 1 + xy$ , which one of the following is true [AMU 1999]  
 (a)  $x > 0, y > 0, z > 0$  (b)  $x > 0, y < 0, 0 < z < 1$  (c)  $x > 0, y < 0, z > 1$  (d)  $x < 0, y < 0, 0 < z < 1$
47. If  $\alpha = 22^\circ 30'$ , then  $(1 + \cos \alpha)(1 + \cos 3\alpha)(1 + \cos 5\alpha)(1 + \cos 7\alpha)$  equals [AMU 1999]  
 (a)  $1/8$  (b)  $1/4$  (c)  $\frac{1 + \sqrt{2}}{2\sqrt{2}}$  (d)  $\frac{\sqrt{2} - 1}{\sqrt{2} + 1}$

### Trigonometrical Ratios of Sum & Difference of Two Angles, Transformation of Product into Sum & Difference, Transformation of Sum & Difference into Product

#### Basic Level

48. If  $A, B, C, D$  are the angles of a cyclic quadrilateral then  $\cos A + \cos B + \cos C + \cos D =$  [IIT 1970]  
 (a)  $2(\cos A + \cos C)$  (b)  $2(\cos A + \cos B)$  (c)  $2(\cos A + \cos D)$  (d) 0
49.  $\frac{\cos 17^\circ + \sin 17^\circ}{\cos 17^\circ - \sin 17^\circ}$  [MP PET 1998 (Similar to EAMCET 1982)]

## Trigonometrical Ratios, Functions and Identities

- (a)  $\tan 62^\circ$  (b)  $\tan 56^\circ$  (c)  $\tan 54^\circ$  (d)  $\tan 73^\circ$
- 50.**  $\cot(45^\circ + \theta)\cot(45^\circ - \theta) =$  [MNR 1973]  
 (a)  $-1$  (b)  $0$  (c)  $1$  (d)  $\infty$
- 51.**  $\tan 75^\circ - \cot 75^\circ =$  [MNR 1982]  
 (a)  $2\sqrt{3}$  (b)  $2 + \sqrt{3}$  (c)  $2 - \sqrt{3}$  (d) None of these
- 52.**  $\sqrt{3} \operatorname{cosec} 20^\circ - \sec 20^\circ =$  [IIT 1988]  
 (a)  $2$  (b)  $\frac{2 \sin 20^\circ}{\sin 40^\circ}$  (c)  $4$  (d)  $\frac{4 \sin 20^\circ}{\sin 40^\circ}$
- 53.**  $\sin 15^\circ + \cos 105^\circ =$  [MP PET 1992]  
 (a)  $0$  (b)  $2 \sin 15^\circ$  (c)  $\cos 15^\circ + \sin 15^\circ$  (d)  $\sin 15^\circ - \cos 15^\circ$
- 54.** If  $\cos(A + B) = \alpha \cos A \cos B + \beta \sin A \sin B$ , then  $(\alpha, \beta) =$  [MP PET 1992]  
 (a)  $(-1, -1)$  (b)  $(-1, 1)$  (c)  $(1, -1)$  (d)  $(1, 1)$
- 55.**  $\cos^2 \alpha + \cos^2(\alpha + 120^\circ) + \cos^2(\alpha - 120^\circ)$  is equal to [MP PET 1993]  
 (a)  $\frac{3}{2}$  (b)  $1$  (c)  $\frac{1}{2}$  (d)  $0$
- 56.** The value of  $\cos 105^\circ + \sin 105^\circ$  is [MNR 1975]  
 (a)  $\frac{1}{2}$  (b)  $1$  (c)  $\sqrt{2}$  (d)  $\frac{1}{\sqrt{2}}$
- 57.**  $\cos^2 48^\circ - \sin^2 12^\circ =$  [MNR 1977]  
 (a)  $\frac{\sqrt{5}-1}{4}$  (b)  $\frac{\sqrt{5}+1}{8}$  (c)  $\frac{\sqrt{3}-1}{4}$  (d)  $\frac{\sqrt{3}+1}{2\sqrt{2}}$
- 58.**  $\sin 20^\circ \sin 40^\circ \sin 60^\circ \sin 80^\circ =$  [MNR 1976, 1981]  
 (a)  $-3/16$  (b)  $5/16$  (c)  $3/16$  (d)  $-5/16$
- 59.**  $\cos 20^\circ \cos 40^\circ \cos 80^\circ =$  [MP PET 1989]  
 (a)  $1/2$  (b)  $1/4$  (c)  $1/6$  (d)  $1/8$
- 60.**  $\cos \frac{2\pi}{15} \cos \frac{4\pi}{15} \cos \frac{8\pi}{15} \cos \frac{16\pi}{15} =$  [IIT 1985]  
 (a)  $1/2$  (b)  $1/4$  (c)  $1/8$  (d)  $1/16$
- 61.** If  $x = \cos 10^\circ \cos 20^\circ \cos 40^\circ$ , then the value of  $x$  is [Roorkee 1995]  
 (a)  $\frac{1}{4} \tan 10^\circ$  (b)  $\frac{1}{8} \cot 10^\circ$  (c)  $\frac{1}{8} \operatorname{cosec} 10^\circ$  (d)  $\frac{1}{8} \sec 10^\circ$
- 62.** The value of  $\cos 52^\circ + \cos 68^\circ + \cos 172^\circ$  is [MP PET 1997]  
 (a)  $0$  (b)  $1$  (c)  $2$  (d)  $\frac{3}{2}$
- 63.**  $\cos 40^\circ + \cos 80^\circ + \cos 160^\circ + \cos 240^\circ =$  [EAMCET 1996]  
 (a)  $0$  (b)  $1$  (c)  $\frac{1}{2}$  (d)  $-\frac{1}{2}$
- 64.**  $1 + \cos 56^\circ + \cos 58^\circ - \cos 66^\circ =$  [IIT 1964]  
 (a)  $2 \cos 28^\circ \cos 29^\circ \cos 33^\circ$  (b)  $4 \cos 28^\circ \cos 29^\circ \cos 33^\circ$  (c)  $4 \cos 28^\circ \cos 29^\circ \sin 33^\circ$  (d)  $2 \cos 28^\circ \cos 29^\circ \sin 33^\circ$
- 65.**  $\cos 15^\circ =$  [MP PET 1998; MNR 1978]



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- (a)  $\sqrt{\frac{1 + \cos 30^\circ}{2}}$  (b)  $\sqrt{\frac{1 - \cos 30^\circ}{2}}$  (c)  $\pm \sqrt{\frac{1 + \cos 30^\circ}{2}}$  (d)  $\pm \sqrt{\frac{1 - \cos 30^\circ}{2}}$
66.  $\tan 5x \tan 3x \tan 2x =$  [EAMCET 1991]  
 (a)  $\tan 5x - \tan 3x - \tan 2x$  (b)  $\frac{\sin 5x - \sin 3x - \sin 2x}{\cos 5x - \cos 3x - \cos 2x}$  (c) 0 (d) None of these
67. If  $\cos \alpha + \cos \beta = 0 = \sin \alpha + \sin \beta$ , then  $\cos 2\alpha + \cos 2\beta =$  [EAMCET 1994]  
 (a)  $-2 \sin(\alpha + \beta)$  (b)  $-2 \cos(\alpha + \beta)$  (c)  $2 \sin(\alpha + \beta)$  (d)  $2 \cos(\alpha + \beta)$
68. If  $\tan A = -\frac{1}{2}$  and  $\tan B = -\frac{1}{3}$ , then  $A+B =$  [IIT 1967; UPSEAT 1987; MP PET 1989]  
 (a)  $\frac{\pi}{4}$  (b)  $\frac{3\pi}{4}$  (c)  $\frac{5\pi}{4}$  (d) None of these
69. If  $\cos(A - B) = \frac{3}{5}$  and  $\tan A \tan B = 2$ , then [MP PET 1997]  
 (a)  $\cos A \cos B = \frac{1}{5}$  (b)  $\sin A \sin B = -\frac{2}{5}$  (c)  $\cos A \cos B = -\frac{1}{5}$  (d)  $\sin A \sin B = -\frac{1}{5}$
70.  $\frac{\sin 3\theta - \cos 3\theta}{\sin \theta + \cos \theta} + 1 =$   
 (a)  $2 \sin 2\theta$  (b)  $2 \cos 2\theta$  (c)  $\tan 2\theta$  (d)  $\cot 2\theta$
71.  $\tan 3A - \tan 2A - \tan A =$  [MNR 1982; Pb. CET 1991]  
 (a)  $\tan 3A \tan 2A \tan A$  (b)  $-\tan 3A \tan 2A \tan A$   
 (c)  $\tan A \tan 2A - \tan 2A \tan 3A - \tan 3A \tan A$  (d) None of these
72. If  $\cos A = m \cos B$ , then [UPSEAT 1990]  
 (a)  $\cot \frac{A+B}{2} = \frac{m+1}{m-1} \tan \frac{B-A}{2}$  (b)  $\tan \frac{A+B}{2} = \frac{m+1}{m-1} \cot \frac{B-A}{2}$   
 (c)  $\cot \frac{A+B}{2} = \frac{m+1}{m-1} \tan \frac{A-B}{2}$  (d) None of these
73. The value of  $\cos 12^\circ + \cos 84^\circ + \cos 156^\circ + \cos 132^\circ$  is [Kerala CEE 1993]  
 (a)  $1/2$  (b) 1 (c)  $-1/2$  (d)  $1/8$
74.  $\tan 100^\circ + \tan 125^\circ + \tan 100^\circ \tan 125^\circ =$  [DCE 1999]  
 (a) 0 (b)  $\frac{1}{2}$  (c) -1 (d) 1
75. If  $\cos P = \frac{1}{7}$  and  $\cos Q = \frac{13}{14}$  where  $P$  and  $Q$  both are acute angles. Then the value of  $P - Q$  is [Orissa JEE 2002; Karnataka CET 2002]  
 (a)  $30^\circ$  (b)  $60^\circ$  (c)  $45^\circ$  (d)  $75^\circ$
76. If  $\sin A = \frac{1}{\sqrt{10}}$  and  $\sin B = \frac{1}{\sqrt{5}}$ , where  $A$  and  $B$  are positive acute angles, then  $A+B =$   
 (a)  $\pi$  (b)  $\frac{\pi}{2}$  (c)  $\frac{\pi}{3}$  (d)  $\frac{\pi}{4}$



77.  $\sin\left(\frac{\pi}{10}\right)\sin\left(\frac{3\pi}{10}\right) =$  [MNR 1984]  
 (a)  $1/2$  (b)  $-1/2$  (c)  $1/4$  (d)  $1$
78.  $\sin 50^\circ - \sin 70^\circ + \sin 10^\circ =$  [MNR 1979]  
 (a)  $1$  (b)  $0$  (c)  $1/2$  (d)  $2$
79. If  $\sin A = \sin B$  and  $\cos A = \cos B$ , then [EAMCET 1994]  
 (a)  $\sin \frac{A-B}{2} = 0$  (b)  $\sin \frac{A+B}{2} = 0$  (c)  $\cos \frac{A-B}{2} = 0$  (d)  $\cos(A+B) = 0$
80.  $\sin 12^\circ \sin 48^\circ \sin 54^\circ =$  [IIT 1982]  
 (a)  $1/16$  (b)  $1/32$  (c)  $1/8$  (d)  $1/4$
81. If  $(1 + \tan \theta)(1 + \tan \phi) = 2$ , then  $\theta + \phi =$  [Karnataka CET 1993]  
 (a)  $30^\circ$  (b)  $45^\circ$  (c)  $60^\circ$  (d)  $75^\circ$
82.  $\cos^2\left(\frac{\pi}{6} + \theta\right) - \sin^2\left(\frac{\pi}{6} - \theta\right) =$  [EAMCET 2001]  
 (a)  $\frac{1}{2} \cos 2\theta$  (b)  $0$  (c)  $-\frac{1}{2} \cos 2\theta$  (d)  $\frac{1}{2}$
83. If  $\sin \theta + \sin 2\theta + \sin 3\theta = \sin \alpha$  and  $\cos \theta + \cos 2\theta + \cos 3\theta = \cos \alpha$ , then  $\theta$  is equal to [AMU 2001]  
 (a)  $\alpha/2$  (b)  $\alpha$  (c)  $2\alpha$  (d)  $\alpha/6$
84.  $\cos \alpha \cdot \sin(\beta - \gamma) + \cos \beta \cdot \sin(\gamma - \alpha) + \cos \gamma \cdot \sin(\alpha - \beta) =$  [EAMCET 2003]  
 (a)  $0$  (b)  $1/2$  (c)  $1$  (d)  $4 \cos \alpha \cos \beta \cos \gamma$
85. Given that  $\cos\left(\frac{\alpha - \beta}{2}\right) = 2 \cos\left(\frac{\alpha + \beta}{2}\right)$ , then  $\tan \frac{\alpha}{2} \tan \frac{\beta}{2}$  is equal to  
 (a)  $\frac{1}{2}$  (b)  $\frac{1}{3}$  (c)  $\frac{1}{4}$  (d)  $\frac{1}{8}$

**Advance Level**

86. If  $\sin A + \sin B = C$ ,  $\cos A + \cos B = D$ , then the value of  $\sin(A + B) =$   
 (a)  $CD$  (b)  $\frac{CD}{C^2 + D^2}$  (c)  $\frac{C^2 + D^2}{2CD}$  (d)  $\frac{2CD}{C^2 + D^2}$
87. If  $A + B = 225^\circ$ , then  $\frac{\cot A}{1 + \cot A} \cdot \frac{\cot B}{1 + \cot B} =$  [MNR 1974]  
 (a)  $1$  (b)  $-1$  (c)  $0$  (d)  $\frac{1}{2}$
88.  $\frac{1}{\sin 10^\circ} - \frac{\sqrt{3}}{\cos 10^\circ} =$  [IIT 1974]  
 (a)  $0$  (b)  $1$  (c)  $2$  (d)  $4$
89.  $\frac{\sin 3\theta + \sin 5\theta + \sin 7\theta + \sin 9\theta}{\cos 3\theta + \cos 5\theta + \cos 7\theta + \cos 9\theta} =$  [Roorkee 1973]  
 (a)  $\tan 3\theta$  (b)  $\cot 3\theta$  (c)  $\tan 6\theta$  (d)  $\cot 6\theta$



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90. If  $\cos(\theta - \alpha)$ ,  $\cos \theta$  and  $\cos(\theta + \alpha)$  are in H.P., then  $\cos \theta \sec \frac{\alpha}{2}$  is equal to [IIT 1997]
- (a)  $\pm \sqrt{2}$                       (b)  $\pm \sqrt{3}$                       (c)  $\pm 1/\sqrt{2}$                       (d) None of these
91.  $\frac{\sin(B+A) + \cos(B-A)}{\sin(B-A) + \cos(B+A)} =$  [Roorkee 1970; IIT 1966]
- (a)  $\frac{\cos B + \sin B}{\cos B - \sin B}$                       (b)  $\frac{\cos A + \sin A}{\cos A - \sin A}$                       (c)  $\frac{\cos A - \sin A}{\cos A + \sin A}$                       (d) None of these
92. If  $\sin 2x = n \sin 2y$ , then the value of  $\frac{\tan(x+y)}{\tan(x-y)}$  is
- (a)  $\frac{n+1}{n-1}$                       (b)  $\frac{n-1}{n+1}$                       (c)  $\frac{1-n}{n+1}$                       (d)  $\frac{1+n}{1-n}$
93. If  $3 \sin \alpha = 5 \sin \beta$ , then  $\frac{\tan \frac{\alpha+\beta}{2}}{\tan \frac{\alpha-\beta}{2}} =$  [EAMCET 1996]
- (a) 1                      (b) 2                      (c) 3                      (d) 4
94. If  $\frac{\pi}{2} < \alpha < \pi$ ,  $\pi < \beta < \frac{3\pi}{2}$ ,  $\sin \alpha = \frac{15}{17}$  and  $\tan \beta = \frac{12}{5}$ , the value of  $\sin(\beta - \alpha)$  is [Roorkee 2000]
- (a)  $\frac{-171}{221}$                       (b)  $\frac{-21}{221}$                       (c)  $\frac{21}{221}$                       (d)  $\frac{17}{221}$
95.  $\cos^2 76^\circ + \cos^2 16^\circ - \cos 76^\circ \cos 16^\circ =$  [EAMCET 2002]
- (a)  $-\frac{1}{4}$                       (b)  $\frac{1}{2}$                       (c) 0                      (d)  $\frac{3}{4}$
96. The value of  $\cos^2 \frac{\pi}{12} + \cos^2 \frac{\pi}{4} + \cos^2 \frac{5\pi}{12}$  is [Karnataka CET 2002]
- (a)  $\frac{3}{2}$                       (b)  $\frac{2}{3}$                       (c)  $\frac{3+\sqrt{3}}{2}$                       (d)  $\frac{2}{3+\sqrt{3}}$
97. If angle  $\theta$  be divided into two parts such that the tangents of one part is  $K$  times the tangent of the other and  $\phi$  is their difference, then  $\sin \theta =$
- (a)  $\frac{K+1}{K-1} \sin \phi$                       (b)  $\frac{K-1}{K+1} \sin \phi$                       (c)  $\frac{2K-1}{2K+1} \sin \phi$                       (d) None of these
98. If  $\tan \alpha, \tan \beta$  are the roots of the equation  $x^2 + px + q = 0$  ( $p \neq 0$ ), then
- (a)  $\sin^2(\alpha + \beta) + p \sin(\alpha + \beta) \cos(\alpha + \beta) + q \cos^2(\alpha + \beta) = q$                       (b)  $\tan(\alpha + \beta) = \frac{p}{q-1}$
- (c)  $\cos(\alpha + \beta) = 1 - q$                       (d)  $\sin(\alpha + \beta) = -p$
99. If  $\tan \alpha$  equals the integral solution of the inequality  $4x^2 - 16x + 15 < 0$  and  $\cos \beta$  equals to the slope of the bisector of first quadrant, then  $\sin(\alpha + \beta) \sin(\alpha - \beta)$  is equal to
- (a)  $\frac{3}{5}$                       (b)  $\frac{-3}{5}$                       (c)  $\frac{2}{\sqrt{5}}$                       (d)  $\frac{4}{5}$
100.  $\frac{\sqrt{2} - \sin \alpha - \cos \alpha}{\sin \alpha - \cos \alpha} =$  [AMU 1999]





- (a)  $\sec\left(\frac{\alpha}{2} - \frac{\pi}{8}\right)$       (b)  $\cos\left(\frac{\pi}{8} - \frac{\alpha}{2}\right)$       (c)  $\tan\left(\frac{\alpha}{2} - \frac{\pi}{8}\right)$       (d)  $\cot\left(\frac{\alpha}{2} - \frac{\pi}{2}\right)$

101. The sum  $S = \sin \theta + \sin 2\theta + \dots + \sin n\theta$ , equals

[AMU 2002]

- (a)  $\sin \frac{1}{2}(n+1)\theta \sin \frac{1}{2}n\theta / \sin \frac{\theta}{2}$   
 (b)  $\cos \frac{1}{2}(n+1)\theta \sin \frac{1}{2}n\theta / \sin \frac{\theta}{2}$   
 (c)  $\sin \frac{1}{2}(n+1)\theta \cos \frac{1}{2}n\theta / \sin \frac{\theta}{2}$   
 (d)  $\cos \frac{1}{2}(n+1)\theta \cos \frac{1}{2}n\theta / \sin \frac{\theta}{2}$

**Trigonometrical Ratios of Multiple and Sub-multiple of an Angle**

**Basic Level**

102.  $2 \cos^2 \theta - 2 \sin^2 \theta = 1$ , then  $\theta =$

[Karnataka CET 1998]

- (a)  $15^\circ$       (b)  $30^\circ$       (c)  $45^\circ$       (d)  $60^\circ$

103. If  $\cos A = \frac{3}{4}$ , then  $32 \sin \frac{A}{2} \cos \frac{5}{2} A =$

[EAMCET 1982]

- (a)  $\sqrt{7}$       (b)  $-\sqrt{7}$       (c) 7      (d) -7

104.  $\cot x - \tan x =$

[MP PET 1986]

- (a)  $\cot 2x$       (b)  $2 \cot^2 x$       (c)  $2 \cot 2x$       (d)  $\cot^2 2x$

105.  $\cos^2 A(3 - 4 \cos^2 A)^2 + \sin^2 A(3 - 4 \sin^2 A)^2 =$

- (a)  $\cos 4A$       (b)  $\sin 4A$       (c) 1      (d) None of these

106.  $2 \sin^2 \beta + 4 \cos(\alpha + \beta) \sin \alpha \sin \beta + \cos 2(\alpha + \beta) =$

[UPSEAT 1993]

- (a)  $\sin 2\alpha$       (b)  $\cos 2\beta$       (c)  $\cos 2\alpha$       (d)  $\sin 2\beta$

107. If  $\tan A = \frac{1 - \cos B}{\sin B}$ , then the value of  $\tan 2A$  in terms of  $\tan B$

- (a)  $\tan 2A = \tan B$       (b)  $\tan 2A = \tan^2 B$       (c)  $\tan 2A = \tan^2 B + 2 \tan B$       (d) None of these

108. If  $\tan A = \frac{1}{2}$ ,  $\tan B = \frac{1}{3}$ , then  $\cos 2A =$

[Karnataka CET 1986, 89]

- (a)  $\sin B$       (b)  $\sin 2B$       (c)  $\sin 3B$       (d) None of these

109. If  $a \cos 2\theta + b \sin 2\theta = c$  has  $\alpha$  and  $\beta$  as its solution, then the value of  $\tan \alpha + \tan \beta$  is

[Haryana CEE 1998]

- (a)  $\frac{c+a}{2b}$       (b)  $\frac{2b}{c+a}$       (c)  $\frac{c-a}{2b}$       (d)  $\frac{b}{c+a}$

110.  $\frac{3 \cos \theta + \cos 3\theta}{3 \sin \theta - \sin 3\theta}$  is equal to

[EAMCET 1996]

- (a)  $1 + \cot^2 \theta$       (b)  $\cot^4 \theta$       (c)  $\cot^3 \theta$       (d)  $2 \cot \theta$

111.  $\sin^2 \frac{\pi}{8} + \sin^2 \frac{3\pi}{8} + \sin^2 \frac{5\pi}{8} + \sin^2 \frac{7\pi}{8} =$

[Karnataka CET 1998]



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- (a) 1 (b) -1 (c) 0 (d) 2
112. If  $k = \sin \frac{\pi}{18} \cdot \sin \frac{5\pi}{18} \cdot \sin \frac{7\pi}{18}$ , then the numerical value of  $k$  is [IIT 1993; UPSEAT 1974]  
 (a) 1/4 (b) 1/8 (c) 1/16 (d) None of these
113.  $\cos \frac{\pi}{7} \cos \frac{2\pi}{7} \cos \frac{4\pi}{7} =$  [MP PET 1998]  
 (a) 0 (b)  $\frac{1}{2}$  (c)  $\frac{1}{4}$  (d)  $-\frac{1}{8}$
114. If  $\cos \theta = \frac{1}{2} \left( a + \frac{1}{a} \right)$ , then the value of  $\cos 3\theta$  is [MP PET 2001]  
 (a)  $\frac{1}{8} \left( a^3 + \frac{1}{a^3} \right)$  (b)  $\frac{3}{2} \left( a + \frac{1}{a} \right)$  (c)  $\frac{1}{2} \left( a^3 + \frac{1}{a^3} \right)$  (d)  $\frac{1}{3} \left( a^3 + \frac{1}{a^3} \right)$
115.  $2 \sin A \cos^3 A - 2 \sin^3 A \cdot \cos A =$  [Roorkee 1975, Kerala (Engg.)  
 2002]  
 (a)  $\sin 4A$  (b)  $\frac{1}{2} \sin 4A$  (c)  $\frac{1}{4} \sin 4A$  (d) None of these
116. If  $\cos A = \frac{3}{4}$ , then  $32 \sin \left( \frac{A}{2} \right) \sin \left( \frac{5A}{2} \right) =$  [DCE 1996]  
 (a) 7 (b) 8 (c) 11 (d) None of these
117. If  $\alpha$  is a root of  $25 \cos^2 \theta + 5 \cos \theta - 12 = 0, \pi/2 < \alpha < \pi$ , then  $\sin 2\alpha$  is equal to [UPSEAT 2001]  
 (a) 24/25 (b) -24/25 (c) 13/18 (d) -13/18

#### Advance Level

118.  $\tan 20^\circ \tan 40^\circ \tan 60^\circ \tan 80^\circ =$  [IIT 1974]  
 (a) 1 (b) 2 (c) 3 (d)  $\sqrt{3}/2$
119. If  $\cos \theta = \frac{3}{5}$  and  $\cos \phi = \frac{4}{5}$ , where  $\theta$  and  $\phi$  are positive acute angles, then  $\cos \frac{\theta - \phi}{2} =$  [MP PET 1988]  
 (a)  $\frac{7}{\sqrt{2}}$  (b)  $\frac{7}{5\sqrt{2}}$  (c)  $\frac{7}{\sqrt{5}}$  (d)  $\frac{7}{2\sqrt{5}}$
120. If  $\cos(\alpha + \beta) = \frac{4}{5}$ ,  $\sin(\alpha - \beta) = \frac{5}{13}$  and  $\alpha, \beta$  lie between 0 and  $\frac{\pi}{4}$ , then  $\tan 2\alpha =$  [IIT 1979; EAMCET  
 2002]  
 (a)  $\frac{16}{63}$  (b)  $\frac{56}{33}$  (c)  $\frac{28}{33}$  (d) None of these
121. If  $x \cos \theta = y \cos \left( \theta + \frac{2\pi}{3} \right) = z \cos \left( \theta + \frac{4\pi}{3} \right)$ , then the value of  $\frac{1}{x} + \frac{1}{y} + \frac{1}{z}$  is equal to [IIT 1984]  
 (a) 1 (b) 2 (c) 0 (d)  $3 \cos \theta$
122. If  $a \tan \theta = b$ , then  $a \cos 2\theta + b \sin 2\theta =$  [EAMCET 1981, 82; MP PET  
 1996]  
 (a)  $a$  (b)  $b$  (c)  $-a$  (d)  $-b$



- 123.** If  $2 \sec 2\alpha = \tan \beta + \cot \beta$ , then one of the values of  $\alpha + \beta$  is  
 (a)  $\frac{\pi}{4}$  (b)  $\frac{\pi}{2}$  (c)  $\pi$  (d)  $2\pi$
- 124.** If  $\cos x + \cos y + \cos \alpha = 0$  and  $\sin x + \sin y + \sin \alpha = 0$ , then  $\cot\left(\frac{x+y}{2}\right) =$  **[Karnataka CET 2001]**  
 (a)  $\sin \alpha$  (b)  $\cos \alpha$  (c)  $\cot \alpha$  (d)  $\sin\left(\frac{x+y}{2}\right)$
- 125.** If  $\sin 2\theta + \sin 2\phi = \frac{1}{2}$  and  $\cos 2\theta + \cos 2\phi = \frac{3}{2}$ , then  $\cos^2(\theta - \phi) =$  **[MP PET 2000]**  
 (a)  $\frac{3}{8}$  (b)  $\frac{5}{8}$  (c)  $\frac{3}{4}$  (d)  $\frac{5}{4}$
- 126.** If  $(\sec \alpha + \tan \alpha)(\sec \beta + \tan \beta)(\sec \gamma + \tan \gamma) = \tan \alpha \tan \beta \tan \gamma$ , then  $(\sec \alpha - \tan \alpha)(\sec \beta - \tan \beta)(\sec \gamma - \tan \gamma) =$  **[Haryana CEE 1998]**  
 (a)  $\cot \alpha \cot \beta \cot \gamma$  (b)  $\tan \alpha \tan \beta \tan \gamma$  (c)  $\cot \alpha + \cot \beta + \cot \gamma$  (d)  $\tan \alpha + \tan \beta + \tan \gamma$
- 127.** If  $\cos 2B = \frac{\cos(A+C)}{\cos(A-C)}$ , then  $\tan A, \tan B, \tan C$  are in  
 (a) A.P (b) G.P (c) H.P (d) None of these
- 128.**  $\left(1 + \cos \frac{\pi}{8}\right)\left(1 + \cos \frac{3\pi}{8}\right)\left(1 + \cos \frac{5\pi}{8}\right)\left(1 + \cos \frac{7\pi}{8}\right) =$  **[IIT 1994; WB JEE 1992]**  
 (a)  $\frac{1}{2}$  (b)  $\frac{1}{4}$  (c)  $\frac{1}{8}$  (d)  $\frac{1}{16}$
- 129.** If  $\frac{\sin^4 A}{a} + \frac{\cos^4 A}{b} = \frac{1}{a+b}$ , then the value of  $\frac{\sin^8 A}{a^3} + \frac{\cos^8 A}{b^3}$  is equal to **[WB JEE 1971]**  
 (a)  $\frac{1}{(a+b)^3}$  (b)  $\frac{a^3 b^3}{(a+b)^3}$  (c)  $\frac{a^2 b^2}{(a+b)^2}$  (d) None of these
- 130.**  $\sqrt{2} + \sqrt{3} + \sqrt{4} + \sqrt{6}$  is equal to **[IIT 1966, 1975]**  
 (a)  $\cot 7\frac{1}{2}^\circ$  (b)  $\sin 7\frac{1}{2}^\circ$  (c)  $\sin 15^\circ$  (d)  $\cos 15^\circ$
- 131.** If  $\sin \beta$  is the geometric mean between  $\sin \alpha$  and  $\cos \alpha$ , then  $\cos 2\beta$  is equal to  
 (a)  $2 \sin^2\left(\frac{\pi}{4} - \alpha\right)$  (b)  $2 \cos^2\left(\frac{\pi}{4} - \alpha\right)$  (c)  $2 \cos^2\left(\frac{\pi}{4} + \alpha\right)$  (d)  $2 \sin^2\left(\frac{\pi}{4} + \alpha\right)$
- 132.** The value of  $k$ , for which  $(\cos x + \sin x)^2 + k \sin x \cos x - 1 = 0$  is an identity, is **[Kerala (Engg.) 2001]**  
 (a) -1 (b) -2 (c) 0 (d) 1
- 133.** If  $\sin^3 x \sin 3x = \sum_{m=0}^n c_m \cos mx$  where  $c_0, c_1, c_2, \dots, c_n$  are constants and  $c_n \neq 0$ , then the value of  $n$  is  
 (a) 15 (b) 6 (c) 1 (d) 0
- 134.** Let  $0 < x < \frac{\pi}{4}$ . Then  $\sec 2x - \tan 2x =$  **[IIT 1994]**  
 (a)  $\tan\left(x - \frac{\pi}{4}\right)$  (b)  $\tan\left(\frac{\pi}{4} - x\right)$  (c)  $\tan\left(x + \frac{\pi}{4}\right)$  (d)  $\tan^2\left(x + \frac{\pi}{4}\right)$

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135. If  $x$  is A.M. of  $\tan \frac{\pi}{9}$  and  $\tan \frac{5\pi}{18}$  and  $y$  is A.M. of  $\tan \frac{\pi}{9}$  and  $\tan \frac{7\pi}{18}$ , then  
 (a)  $x > y$  (b)  $x = y$  (c)  $2x = y$  (d)  $x = 2y$
136. If  $\cos^4 \theta \sec^2 \alpha, \frac{1}{2}$  and  $\sin^4 \theta \operatorname{cosec}^2 \alpha$  are in A.P., then  $\cos^8 \theta \sec^6 \alpha, \frac{1}{2}$  and  $\sin^8 \theta \operatorname{cosec}^6 \alpha$  are in  
 (a) A.P. (b) G.P. (c) H.P. (d) None of these
137. Let  $f_n(\theta) = \tan \frac{\theta}{2}(1 + \sec \theta)(1 + \sec 2\theta)(1 + \sec 4\theta) \dots (1 + \sec 2^n \theta)$ . Then [IIT Screening 1999; 2001]  
 (a)  $f_2\left(\frac{\pi}{16}\right) = 1$  (b)  $f_3\left(\frac{\pi}{32}\right) = 1$  (c)  $f_4\left(\frac{\pi}{64}\right) = 1$  (d) All of these
138. If A, B, C, D are the smallest positive angles in ascending order of magnitude which have their sines equal to the positive quantity  $k$ , then the value of  $4 \sin \frac{A}{2} + 3 \sin \frac{B}{2} + 2 \sin \frac{C}{2} + \sin \frac{D}{2}$  is equal to  
 (a)  $2\sqrt{1-k}$  (b)  $2\sqrt{1+k}$  (c)  $2\sqrt{k}$  (d) None of these
139. If  $\alpha, \beta$  are different values of  $x$  satisfying  $a \cos x + b \sin x = c$ , then  $\tan\left(\frac{\alpha + \beta}{2}\right) =$  [Orissa JEE 2003; EAMCET 1986]  
 (a)  $a + b$  (b)  $a - b$  (c)  $\frac{b}{a}$  (d)  $\frac{a}{b}$

### Maximum and Minimum value

#### Basic Level

140. The maximum value of  $a \cos x + b \sin x$  is [MNR 1991; MP PET 1999]  
 (a)  $a + b$  (b)  $a - b$  (c)  $|a| + |b|$  (d)  $(a^2 + b^2)^{1/2}$
141. The minimum value of  $\cos \theta + \sin \theta$  is [MNR 1976]  
 (a) 0 (b)  $-\sqrt{2}$  (c)  $1/2$  (d)  $\sqrt{2}$
142. The minimum value of  $3 \cos x + 4 \sin x + 8$  is [UPSEAT 1991]  
 (a) 5 (b) 9 (c) 2 (d) 3
143. If  $\theta$  is an acute angle and  $\sin \theta = \frac{p-6}{8-p}$ , then  $p$  must satisfy  
 (a)  $6 \leq p < 8$  (b)  $6 \leq p < 7$  (c)  $3 \leq p \leq 4$  (d)  $4 \leq p < 7$

#### Advance Level

144. Maximum value of  $\cos^2 x + \cos^2 y - \cos^2 z$  is  
 (a) 0 (b) 1 (c) 3 (d) 2
145. Let  $n$  be a positive integer such that  $\sin\left(\frac{\pi}{2^n}\right) + \cos\left(\frac{\pi}{2^n}\right) = \frac{\sqrt{n}}{2}$ , then

- (a)  $6 \leq n \leq 8$                       (b)  $4 < n \leq 8$                       (c)  $4 \leq n < 8$                       (d)  $4 < n < 8$
146. If  $\alpha \in \left(0, \frac{\pi}{2}\right)$ , then  $\sqrt{x^2+x} + \frac{\tan^2 \alpha}{\sqrt{x^2+x}}$  is always greater than or equal to [IIT Screening 2003]
- (a)  $2 \tan \alpha$                       (b) 1                      (c) 2                      (d)  $\sec^2 \alpha$
147. The maximum value of  $(\cos \alpha_1)(\cos \alpha_2)\dots(\cos \alpha_n)$ , under the restrictions,  $0 \leq \alpha_1, \alpha_2, \dots, \alpha_n \leq \frac{\pi}{2}$  and  $(\cot \alpha_1)(\cot \alpha_2)\dots(\cot \alpha_n) = 1$  is [IIT Screening 2001]
- (a)  $\frac{1}{2^{n/2}}$                       (b)  $\frac{1}{2^n}$                       (c)  $\frac{1}{2n}$                       (d) 1
148. Let  $f(\theta) = \sin \theta(\sin \theta + \sin 3\theta)$ . Then [IIT Screening 2000]
- (a)  $f(\theta) \geq 0$  only when  $\theta \geq 0$                       (b)  $f(\theta) \leq 0$  only when  $\theta \leq 0$   
 (c)  $f(\theta) \geq 0$  for all real  $\theta$                       (d) None of these
149. The minimum value of  $2^{\sin x} + 2^{\cos x}$  is
- (a) 1                      (b) 2                      (c)  $2^{-\frac{1}{\sqrt{2}}}$                       (d)  $2^{1-\frac{1}{\sqrt{2}}}$

**Conditional Trigonometrical Identities**

**Basic Level**

150. If  $A + B + C = \pi$ , then  $\frac{\tan A + \tan B + \tan C}{\tan A \tan B \tan C} =$  [EAMCET 1989]
- (a) 0                      (b) 2                      (c) 1                      (d) -1
151. If  $A + B + C = \pi$  and  $\cos A = \cos B \cos C$ , then  $\tan B \tan C$  is equal to [AMU 2001]
- (a)  $\frac{1}{2}$                       (b) 2                      (c) 1                      (d)  $-\frac{1}{2}$

**Advance Level**

152. If  $\alpha + \beta - \gamma = \pi$ , then  $\sin^2 \alpha + \sin^2 \beta - \sin^2 \gamma =$  [IIT 1980]
- (a)  $2 \sin \alpha \sin \beta \cos \gamma$                       (b)  $2 \cos \alpha \cos \beta \cos \gamma$                       (c)  $2 \sin \alpha \sin \beta \sin \gamma$                       (d) None of these
153. If  $A + B + C = \frac{3\pi}{2}$ , then  $\cos 2A + \cos 2B + \cos 2C + 4 \sin A \sin B \sin C =$  [EAMCET 2003; 1989]
- (a) 0                      (b) 1                      (c) 2                      (d) 3
154. If  $A, B, C$  are the angles of a triangle, then  $\sin^2 A + \sin^2 B + \sin^2 C - 2 \cos A \cos B \cos C =$  [Karnataka CET 1989]
- (a) 1                      (b) 2                      (c) 3                      (d) 4

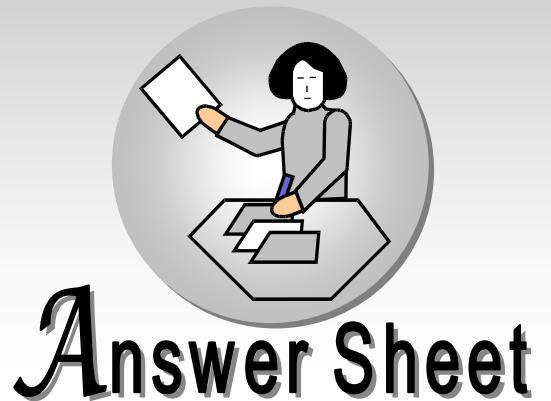


**44** Trigonometrical Ratios, Functions and

155. If  $\alpha + \beta = \frac{\pi}{2}$  and  $\beta + \gamma = \alpha$ , then  $\tan \alpha$  equals [IIT Screening 2001]
- (a)  $2(\tan \beta + \tan \gamma)$       (b)  $\tan \beta + \tan \gamma$       (c)  $\tan \beta + 2 \tan \gamma$       (d)  $2 \tan \beta + \tan \gamma$
156. Let  $A, B$  and  $C$  are the angles of a plain triangle and  $\tan \frac{A}{2} = \frac{1}{3}$ ,  $\tan \frac{B}{2} = \frac{2}{3}$ . Then  $\tan \frac{C}{2}$  is equal to
- (a)  $7/9$       (b)  $2/9$       (c)  $1/3$       (d)  $2/3$

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*Trigonometrical Ratios, Functions and Assignment (Basic & Advance Level)*

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
b	b	b	d	b	d	a	c	a	b	a	b	c	a	b	c	c	c	c	c
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
b	d	a	a	b	a	d	a	c	b,d	d	c	c	b	b	a	a	d	d	d
41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
a	a	c	c	b	b	a	d	a	c	a	c	a	c	a	d	b	c	d	d
61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80
b	a	d	c	a	a	b	b	a	a	a	a	c	d	b	d	c	b	a	c

Trigonometrical Ratios, Functions and Identities

81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
b	a	a	a	b	d	d	d	c	a	b	a	d	d	d	a	a	a, b	d	c
101	102	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120
a	b	b	c	c	c	a	b	b	c	d	b	d	c	b	c	b	c	b	b
121	122	123	124	125	126	127	128	129	130	131	132	133	134	135	136	137	138	139	140
c	a	a	c	b	a	b	c	a	a	a, c	b	b	b	c	a	d	b	c	d
141	142	143	144	145	146	147	148	149	150	151	152	153	154	155	156				
b	d	b	d	b	a	a	c	d	c	b	a	b	b	c	a				

